

BVI Case Study

Karen Nershi

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BVI Case Study

The following code generates output for Tables 5-6 in the main body of the paper; it also generates output for Tables 10-12 and Figures 3-4 in the Supplementary Material. This output matches the code included in the file “BVI Case Study.R.”

```
#####  
##### PART 1: LOAD PACKAGES AND FUNCTIONS FOR ANALYSIS #####  
#####  
  
#####  
### A. PACKAGES  
  
# Packages used in analysis  
pkg = c("tidyverse", "stargazer", "knitr", "kableExtra", "lmtest", "sandwich")  
  
# Checks if installed; if not, install  
if (length(setdiff(pkg, rownames(installed.packages()))) > 0) {  
  install.packages(setdiff(pkg, rownames(installed.packages())))  
}  
  
# Load packages  
suppressMessages(suppressWarnings(lapply(pkg, library, character.only = TRUE)))  
  
## [[1]]  
## [1] "lubridate" "forcats" "stringr" "dplyr" "purrr" "readr"  
## [7] "tidyr" "tibble" "ggplot2" "tidyverse" "stats" "graphics"  
## [13] "grDevices" "utils" "datasets" "methods" "base"  
##  
## [[2]]  
## [1] "stargazer" "lubridate" "forcats" "stringr" "dplyr" "purrr"  
## [7] "readr" "tidyr" "tibble" "ggplot2" "tidyverse" "stats"  
## [13] "graphics" "grDevices" "utils" "datasets" "methods" "base"  
##  
## [[3]]  
## [1] "knitr" "stargazer" "lubridate" "forcats" "stringr" "dplyr"  
## [7] "purrr" "readr" "tidyr" "tibble" "ggplot2" "tidyverse"  
## [13] "stats" "graphics" "grDevices" "utils" "datasets" "methods"  
## [19] "base"  
##  
## [[4]]  
## [1] "kableExtra" "knitr" "stargazer" "lubridate" "forcats"  
## [6] "stringr" "dplyr" "purrr" "readr" "tidyr"
```

```
## [11] "tibble"      "ggplot2"      "tidyverse"    "stats"        "graphics"
## [16] "grDevices"   "utils"        "datasets"     "methods"      "base"
##
## [[5]]
## [1] "lmtest"      "zoo"          "kableExtra"   "knitr"        "stargazer"
## [6] "lubridate"   "forcats"     "stringr"      "dplyr"        "purrr"
## [11] "readr"       "tidyr"       "tibble"       "ggplot2"     "tidyverse"
## [16] "stats"       "graphics"    "grDevices"    "utils"        "datasets"
## [21] "methods"     "base"
##
## [[6]]
## [1] "sandwich"    "lmtest"      "zoo"          "kableExtra"   "knitr"
## [6] "stargazer"   "lubridate"   "forcats"     "stringr"      "dplyr"
## [11] "purrr"       "readr"       "tidyr"       "tibble"       "ggplot2"
## [16] "tidyverse"   "stats"       "graphics"    "grDevices"    "utils"
## [21] "datasets"    "methods"     "base"
```

```
rm(list=ls())
```

```
#####
```

```
### B. FUNCTIONS
```

```
# Create a function that will prepare data given range of interest
```

```
process_trading_data <- function(df1, lower_bound, upper_bound) {
  require(dplyr)
```

```
# Filter data based on bounds
```

```
df <- filter(df1, base > lower_bound & base < upper_bound)
```

```
# Create a function to round the dollar values down to the nearest 10
```

```
round_down <- function(numbers) {
  rounded_numbers <- floor(numbers / 10) * 10
  return(rounded_numbers)
}
```

```
# Apply function to dollar values to identify bins
```

```
df$dollar_bins <- round_down(df$base)
```

```
# Create an identifier for each exchange-trading pair
```

```
df$identifier <- paste0(df$s, "_", df$exchange, "_", df$type)
```

```
# Identify treated entities
```

```
treated_entities <- unique(select(filter(df, type == "regulated"), identifier))
```

```
# Summarize the total trades by day, bin, and exchange-trading pair
```

```
df2 <- df %>%
  group_by(m_d, dollar_bins, identifier) %>%
  summarise(total_trades = n(), .groups = "drop")
```

```
# Create a new dataframe that identifies all day-bin-exchange-trading pair combinations
```

```
m_d <- unique(df$m_d)
bins_in_range <- unique(df$dollar_bins)
id_list <- unique(df$identifier)
```

```

# Create complete combination grid
df3 <- expand.grid(m_d = m_d, dollar_bins = bins_in_range, identifier = id_list)

# Merge this with your summarized data
df4 <- df3 %>%
  left_join(df2, by = c("m_d", "dollar_bins", "identifier"))

# Fills NAs in total_trades with zeros
df4$total_trades <- ifelse(is.na(df4$total_trades), 0, df4$total_trades)

# Create a new variable for all daily trades within the range for each exchange-trading pair
df4 <- df4 %>%
  group_by(m_d, identifier) %>%
  mutate(daily_trades_range = sum(total_trades)) %>%
  ungroup()

# Create a new variable for the proportion of trades within each bin divided by all daily trades
# If all daily trades within the range for an exchange-trading pair is zero, set prop_trades to zero
df4$prop_trades <- ifelse(df4$daily_trades_range == 0, 0,
  df4$total_trades / df4$daily_trades_range)

### DID Specific variables
# Create a variable for treated units
df4$treat <- ifelse(df4$identifier %in% treated_entities$identifier, 1, 0)

# Create a variable for the post-treatment period
df4$time <- ifelse(df4$m_d > "07:09", 1, 0)

# Create a variable to identify each bin for each exchange-trading pair
df4$id_2 <- paste0(df4$identifier, "_", df4$dollar_bins)

return(df4)
}

# Create function for estimating bunching
estimate_beta = function(thedata, z_vector, binv, zstar, bins_excl_l, bins_excl_r, rates) {
  z_vector = thedata$base

  # set parameters
  binwidth = 10 # 10 units for each bin
  bins_l = 25
  bins_r = 25
  poly = 3 # degree of polynomial
  n_boot = 1000 # number of iterations for calculating bootstrapped standard errors
  rn = NA
  correct_above_zu = FALSE

  zmax <- zstar + (binwidth * bins_r)
  zmin <- zstar - (binwidth * bins_l)
  bins <- seq(zmin, zmax, by = binwidth)

  ##Cut the bins

```

```

thebin <- cut(z_vector, bins, right = FALSE, labels = FALSE)
thebin <- zmin + binwidth * (thebin - 1)
thedata <- data.frame(z = z_vector, bin = thebin)
thedata <- thedata %>% dplyr::group_by(bin) %>%
  dplyr::summarise(freq = n(), z = mean(z, na.rm = TRUE)) %>%
  dplyr::filter(!is.na(bin))
thedata$freq_orig <- thedata$freq
thedata <- as.data.frame(thedata)

data_binned = thedata

data_binned$z_rel = (data_binned$bin - zstar)/binwidth
data_binned$zstar <- ifelse(data_binned$bin == zstar, 1,
  0)
extra_fe_vector <- ""

polynomial_vector <- c()
for (i in seq(poly)) {
  poly_varname <- paste0("poly_", i)
  data_binned[[poly_varname]] <- data_binned$z^i
  polynomial_vector <- c(polynomial_vector, poly_varname)
}
bins_excl_l_all <- c()
if (bins_excl_l != 0) {
  bins_excl_l_vector <- c()
  for (i in seq(bins_excl_l)) {
    bins_excl_l_varname <- paste0("bin_excl_l_", i)
    data_binned[[bins_excl_l_varname]] <- ifelse(data_binned$z_rel ==
      -i, 1, 0)
    bins_excl_l_vector <- c(bins_excl_l_vector, bins_excl_l_varname)
  }
  bins_excl_l_all <- c(bins_excl_l_all, bins_excl_l_vector)
}
if (bins_excl_r != 0) {
  bins_excl_r_vector <- c()
  for (i in seq(bins_excl_r)) {
    bin_excl_r_varname <- paste0("bin_excl_r_", i)
    data_binned[[bin_excl_r_varname]] <- ifelse(data_binned$z_rel ==
      i, 1, 0)
    bins_excl_r_vector <- c(bins_excl_r_vector, bin_excl_r_varname)
  }
  bins_excl_r_all <- c(bins_excl_r_all, bins_excl_r_vector)
}
if (length(bins_excl_all) > 0) {
  data_binned$bunch_region <- rowSums(data_binned[, c("zstar",
    bins_excl_all)])
}
data_binned$bin_above_excluded <- ifelse(data_binned$bin >
  zstar, 1, 0)
rn_vector <- ""
rhs_vars <- c("zstar", extra_fe_vector, polynomial_vector,
  rn_vector, bins_excl_all)
rhs_vars <- setdiff(rhs_vars, "")

```

```

model_formula <- stats::as.formula(paste0("freq", " ~ ",
                                         paste(rhs_vars, collapse = " +")))

data_forreg <- list(data_binned = data_binned, model_formula = model_formula)

#####
thedata = data_forreg$data_binned
themodelformula = data_forreg$model_formula
notch = FALSE
zD_bin = NA

# Define model outcomes
model_fit <- stats::lm(themodelformula, thedata)
coefficients <- summary(model_fit)$coefficients
residuals <- stats::residuals(model_fit)
thedata$cf <- stats::predict(model_fit, thedata)
thedata$cf <- thedata$cf - (thedata$zstar * coefficients["zstar",
                                                         "Estimate"])

bins_excluded_in_reg <- rownames(coefficients)[grepl("bin_excl",
                                                    rownames(coefficients))]

for (i in bins_excluded_in_reg) {
  thedata$cf <- thedata$cf - (thedata[[i]] * coefficients[i,
                                                         "Estimate"])
}

bins_zstar_zu <- sum(grepl("bin_excl_r", rownames(coefficients)))
bins_zl_zstar <- sum(grepl("bin_excl_l", rownames(coefficients))) +
  1
zstarvalue <- thedata$bin[thedata$zstar == 1]
zstarvalue = zstarvalue[1]
binwidthvalue <- thedata$bin[2] - thedata$bin[1]

#Excluded bins below threshold
thedata$zl_zstar <- ifelse(((thedata$bin >=
                           (zstarvalue -
                            (binwidthvalue * (bins_zl_zstar - 1)))) &
                           (thedata$bin <= zstarvalue)),
                          1, 0)
thedata$zstar_zu <- ifelse((thedata$bin <=
                           zstarvalue + (binwidthvalue *
                                           bins_zstar_zu)) &
                           (thedata$bin > zstarvalue), 1, 0)
thedata$bunch_region <- ifelse(thedata$zl_zstar == 1, "zl_zstar",
                              ifelse(thedata$zstar_zu == 1,
                                       "zstar_zu", "outside_bunching"))
bunching_region_count <- thedata %>% dplyr::group_by(bunch_region) %>%
  dplyr::summarize(actual = sum(freq_orig), cf = sum(cf),
                  excess = actual - cf)

B_zl_zstar <- as.numeric(subset(bunching_region_count, bunch_region ==
                              "zl_zstar", select = 'excess'))
B_zstar_zu <- as.numeric(subset(bunching_region_count, bunch_region ==
                              "zstar_zu", select = "excess"))

if (is.na(B_zstar_zu)) {

```

```

  B_zstar_zu <- 0
}
bunching_excess <- B_zl_zstar + B_zstar_zu
cf_bunching <- sum(subset(bunching_region_count, bunch_region !=
                          "outside_bunching", select = "cf"))
bins_bunching <- sum(thedata$bunch_region %in% c("zl_zstar",
                                                "zstar_zu"))
c0 <- cf_bunching/bins_bunching
b_estimate <- as.numeric(sprintf("%.3f", bunching_excess/c0))

##Calculate standard errors
data_for_boot <- thedata
model <- themodelformula

boot_results <- sapply(seq(1:n_boot), function(i) {
  data_for_boot$freq_orig <- data_for_boot$freq_orig +
    sample(residuals, replace = TRUE)
  data_for_boot$freq <- data_for_boot$freq_orig
  booted_firstpass <- bunching::fit_bunching(data_for_boot,
                                             model, binwidth, notch, zD_bin)
})
set.seed(99)
ans = list()
extract_me <- function(boot_results, ans) {
  thelist = seq(7, 12994, 13)
  for (i in thelist) {
    a = boot_results[[i]]
    ans <- append(ans, a)
  }
  return(ans)
}

betas = extract_me(boot_results = boot_results, ans = ans)
betas = unlist(betas, use.names=FALSE)
b_sd <- stats::sd(betas, na.rm = TRUE)

#####Create df
info = cbind.data.frame(b_estimate, b_sd)
names(info) = c('beta', 'standard error')
info$threshold = zstar
info <- info[,c(3,1:2)]
return(info)
}

# Create a function to round values within a column
rounding = function(x) {
  A = round(x,digits=3)
  return(A)
}

#####
##### PART 2: ANALYSIS #####

```

```
#####

#####
### TABLE 5
#####

# Set working directory to location of data files
# setwd("path to files")
setwd("/Users/knershi@middlebury.edu/Documents/Temporary/")

## Part 1: Data preparation

# Import data
df.btc <- read.csv("full.BVI.btc.csv")
df.eth <- read.csv("full.BVI.eth.csv")

# Subset data to pre-period
df.btc_pre <- df.btc %>%
  filter(m_d < "07:10")
df.eth_pre <- df.eth %>%
  filter(m_d < "07:10")

# Prep the data using the function
lower_bound = 749
upper_bound = 1250
p.btc <- process_trading_data(df.btc_pre, lower_bound = lower_bound, upper_bound = upper_bound)
p.eth <- process_trading_data(df.eth_pre, lower_bound = lower_bound, upper_bound = upper_bound)

## Part 2: Prepare descriptive statistics

# Identify Bitcoin vs. Ethereum transactions

# Calculate N exchanges
N_exchanges <- c(length(unique(df.btc[(df.btc$type=="regulated"),]$exchange)),
  length(unique(df.btc[(df.btc$type=="unregulated"),]$exchange)),
  length(unique(df.eth[(df.eth$type=="regulated"),]$exchange)),
  length(unique(df.eth[(df.eth$type=="unregulated"),]$exchange))
)

# Calculate N trading pairs
N_trading_pairs <- c(length(unique(p.btc[(p.btc$treat==1),]$identifier)),
  length(unique(p.btc[(p.btc$treat==0),]$identifier)),
  length(unique(p.eth[(p.eth$treat==1),]$identifier)),
  length(unique(p.eth[(p.eth$treat==0),]$identifier)))

# Calculate N transactions
N_transactions <- c(nrow(df.btc[(df.btc$type=="regulated"),]),
  nrow(df.btc[(df.btc$type=="unregulated"),]),
  nrow(df.eth[(df.eth$type=="regulated"),]),
  nrow(df.eth[(df.eth$type=="unregulated"),]))

## Difference in means t-test
```

```

# 1 bin below the threshold

# T.test difference in means
t1 <- t.test(p.btc[(p.btc$treat==1 & p.btc$dollar_bins==990),]$prop_trades, p.btc[(p.btc$treat==0 & p.btc$dollar_bins==990),]$prop_trades)
means_t1 <- c(round(t1$estimate[1],3),round(t1$estimate[2],3))

t2 <- t.test(p.eth[(p.eth$treat==1 & p.eth$dollar_bins==990),]$prop_trades, p.eth[(p.eth$treat==0 & p.eth$dollar_bins==990),]$prop_trades)
means_t2 <- c(round(t2$estimate[1],3),round(t2$estimate[2],3))

# 5 bins below the threshold

## T.test range of interest
t3 <- t.test(p.btc[(p.btc$treat==1 & p.btc$dollar_bins > 940 & p.btc$dollar_bins < 1000),]$prop_trades, p.btc[(p.btc$treat==0 & p.btc$dollar_bins > 940 & p.btc$dollar_bins < 1000),]$prop_trades)
means_t3 <- c(round(t3$estimate[1],3),round(t3$estimate[2],3))

t4 <- t.test(p.eth[(p.eth$treat==1 & p.eth$dollar_bins > 940 & p.eth$dollar_bins < 1000),]$prop_trades, p.eth[(p.eth$treat==0 & p.eth$dollar_bins > 940 & p.eth$dollar_bins < 1000),]$prop_trades)
means_t4 <- c(round(t4$estimate[1],3),round(t4$estimate[2],3))

## Bind this info into one data frame and display

# Combine means into rows
means_1 <- c(means_t1,means_t2)
means_2 <- c(means_t3,means_t4)

table_df <- rbind.data.frame(N_exchanges,
                             N_trading_pairs,
                             N_transactions,
                             means_1,
                             means_2)

names(table_df) <- c("BVI (btc)","Unregulated (btc)","BVI (eth)","Unregulated (eth)")
rownames(table_df) <- c("N_exchanges","N_trading_pairs","N_transactions",
                       "Mean Proportion of Trades 1 Bin Below Threshold",
                       "Mean Proportion of Trades 5 Bins Below Threshold")

table_df$`P-values (btc)` <- c("", "", "", round(t1$p.value,3), round(t3$p.value,3))
table_df$`P-values (eth)` <- c("", "", "", round(t2$p.value,3), round(t4$p.value,3))

print(table_df)

```

```

##                               BVI (btc) Unregulated (btc)
## N_exchanges                   2.000           4.000
## N_trading_pairs                4.000           4.000
## N_transactions                1126824.000       1727534.000
## Mean Proportion of Trades 1 Bin Below Threshold    0.096           0.024
## Mean Proportion of Trades 5 Bins Below Threshold    0.038           0.016
##                               BVI (eth) Unregulated (eth)
## N_exchanges                   2.000           3.000
## N_trading_pairs                2.000           3.000
## N_transactions                597561.000       925938.000
## Mean Proportion of Trades 1 Bin Below Threshold    0.027           0.031
## Mean Proportion of Trades 5 Bins Below Threshold    0.024           0.018
##                               P-values (btc) P-values (eth)
## N_exchanges

```

```

## N_trading_pairs
## N_transactions
## Mean Proportion of Trades 1 Bin Below Threshold          0          0.727
## Mean Proportion of Trades 5 Bins Below Threshold          0          0.059
#####
### TABLE 6
#####

# To avoid confusion, remove all objects created for previous table
# Define a list of prefixes you want to remove
prefixes_to_remove <- c("p.btc","p.eth",
                        "df.btc_pre","df.eth_pre")

# Create a pattern that matches any of these prefixes at the beginning of object names
pattern <- paste0("^(", paste(prefixes_to_remove, collapse="|"), ")")

# Remove objects matching the pattern
rm(list=ls(pattern=pattern))

# Prep the data using the function
lower_bound = 749
upper_bound = 1250
p.btc <- process_trading_data(df.btc, lower_bound = lower_bound, upper_bound = upper_bound)
p.eth <- process_trading_data(df.eth, lower_bound = lower_bound, upper_bound = upper_bound)

## Create two ranges of 50 and 10 dollars below the threshold for each
btc_range1 <- filter(p.btc, dollar_bins > 949 & dollar_bins < 1000)
btc_range2 <- filter(p.btc, dollar_bins > 989 & dollar_bins < 1000)

eth_range1 <- filter(p.eth, dollar_bins > 949 & dollar_bins < 1000)
eth_range2 <- filter(p.eth, dollar_bins > 989 & dollar_bins < 1000)

# Create difference-in-differences models for each range
btc_mod1 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),btc_range1)
btc_mod2 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),btc_range2)

eth_mod1 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),eth_range1)
eth_mod2 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),eth_range2)

## Extract R^2, adjusted R^2, and N for each model
# mod1
b_mod1_r2 <- round(summary(btc_mod1)$r.squared,3)
b_mod1_adj.r2 <- round(summary(btc_mod1)$adj.r.squared,3)
b_N1 <- nrow(btc_range1)

# mod2
b_mod2_r2 <- round(summary(btc_mod2)$r.squared,3)
b_mod2_adj.r2 <- round(summary(btc_mod2)$adj.r.squared,3)
b_N2 <- nrow(btc_range2)

# mod1
e_mod1_r2 <- round(summary(eth_mod1)$r.squared,3)
e_mod1_adj.r2 <- round(summary(eth_mod1)$adj.r.squared,3)

```

```

e_N1 <- nrow(eth_range1)

# mod2
e_mod2_r2 <- round(summary(eth_mod2)$r.squared,3)
e_mod2_adj.r2 <- round(summary(eth_mod2)$adj.r.squared,3)
e_N2 <- nrow(eth_range2)

# Now calculate models for each range using robust standard errors
# clustered by exchange - trading pair
b_mod_robust <- coeftest(btc_mod1, vcov = vcovHC(btc_mod1, type="HC1"),
                        cluster = ~identifier)
b_mod_robust2 <- coeftest(btc_mod2, vcov = vcovHC(btc_mod2, type="HC1"),
                        cluster = ~identifier)

e_mod_robust <- coeftest(eth_mod1, vcov = vcovHC(eth_mod1, type="HC1"),
                        cluster = ~identifier)
e_mod_robust2 <- coeftest(eth_mod2, vcov = vcovHC(eth_mod2, type="HC1"),
                        cluster = ~identifier)

# Now use stargazer to create a Latex table using this information
stargazer(b_mod_robust,b_mod_robust2,
          e_mod_robust,e_mod_robust2,
          type = "text",
          omit=c("m_d","id_2"),
          star.cutoffs = c(0.05, 0.01, 0.001),
          add.lines = list(c("N",b_N1,b_N2,e_N1,e_N2),
                          c("R squared", b_mod1_r2, b_mod2_r2,
                            e_mod1_r2, e_mod2_r2),
                          c("Adjusted R squared", b_mod1_adj.r2,
                            b_mod2_adj.r2, e_mod1_adj.r2, e_mod2_adj.r2)))

```

```

##
## =====
##                               Dependent variable:
##                               -----
##                               (1)      (2)      (3)      (4)
## -----
## treat                        -0.010  0.182*** -0.004  -0.026*
##                               (0.006) (0.026) (0.004) (0.011)
##
## time                         -0.012  -0.011  -0.009  -0.023
##                               (0.010) (0.036) (0.007) (0.017)
##
## treat:time                   0.018*** 0.076*** 0.011** 0.028**
##                               (0.005) (0.019) (0.003) (0.010)
##
## Constant                     0.014   -0.013  0.017*  0.034*
##                               (0.009) (0.030) (0.007) (0.017)
##
## -----
## N                             2040     408     1275     255
## R squared                     0.56     0.618   0.355     0.51
## Adjusted R squared            0.54     0.555   0.314     0.375

```

```

## =====
## Note:                *p<0.05; **p<0.01; ***p<0.001
#####
### TABLE 10
#####

# To avoid confusion, remove all objects created for previous table
# Define a list of prefixes you want to remove
prefixes_to_remove <- c("p.btc","p.eth",
                        "b_","e_",
                        "btc_","eth_",
                        "lower_","upper_")

# Create a pattern that matches any of these prefixes at the beginning of object names
pattern <- paste0("^(", paste(prefixes_to_remove, collapse="|"), ")")

# Remove objects matching the pattern
rm(list=ls(pattern=pattern))

# Prep the data using the function
lower_bound = 249
upper_bound = 750
p.btc <- process_trading_data(df.btc, lower_bound = lower_bound, upper_bound = upper_bound)
p.eth <- process_trading_data(df.eth, lower_bound = lower_bound, upper_bound = upper_bound)

## Create two ranges of 50 and 10 dollars below the threshold for each
btc_range1 <- filter(p.btc, dollar_bins > 449 & dollar_bins < 500)
btc_range2 <- filter(p.btc, dollar_bins > 489 & dollar_bins < 500)

eth_range1 <- filter(p.eth, dollar_bins > 449 & dollar_bins < 500)
eth_range2 <- filter(p.eth, dollar_bins > 489 & dollar_bins < 500)

# Create difference-in-differences models for each range
btc_mod1 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),btc_range1)
btc_mod2 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),btc_range2)

eth_mod1 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),eth_range1)
eth_mod2 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),eth_range2)

## Extract R^2, adjusted R^2, and N for each model
# mod1
b_mod1_r2 <- round(summary(btc_mod1)$r.squared,3)
b_mod1_adj.r2 <- round(summary(btc_mod1)$adj.r.squared,3)
b_N1 <- nrow(btc_range1)

# mod2
b_mod2_r2 <- round(summary(btc_mod2)$r.squared,3)
b_mod2_adj.r2 <- round(summary(btc_mod2)$adj.r.squared,3)
b_N2 <- nrow(btc_range2)

# mod1
e_mod1_r2 <- round(summary(eth_mod1)$r.squared,3)
e_mod1_adj.r2 <- round(summary(eth_mod1)$adj.r.squared,3)

```

```

e_N1 <- nrow(eth_range1)

# mod2
e_mod2_r2 <- round(summary(eth_mod2)$r.squared,3)
e_mod2_adj.r2 <- round(summary(eth_mod2)$adj.r.squared,3)
e_N2 <- nrow(eth_range2)

# Now calculate models for each range using robust standard errors
# clustered by exchange - trading pair
b_mod_robust <- coeftest(btc_mod1, vcov = vcovHC(btc_mod1, type="HC1"),
                        cluster = ~identifier)
b_mod_robust2 <- coeftest(btc_mod2, vcov = vcovHC(btc_mod2, type="HC1"),
                        cluster = ~identifier)

e_mod_robust <- coeftest(eth_mod1, vcov = vcovHC(eth_mod1, type="HC1"),
                        cluster = ~identifier)
e_mod_robust2 <- coeftest(eth_mod2, vcov = vcovHC(eth_mod2, type="HC1"),
                        cluster = ~identifier)

# Now use stargazer to create a Latex table using this information
stargazer(b_mod_robust,b_mod_robust2,
          e_mod_robust,e_mod_robust2,
          type="text",
          omit=c("m_d","id_2"),
          star.cutoffs = c(0.05, 0.01, 0.001),
          add.lines = list(c("N",b_N1,b_N2,e_N1,e_N2),
                          c("R squared", b_mod1_r2, b_mod2_r2, e_mod1_r2,
                              e_mod2_r2),
                          c("Adjusted R squared", b_mod1_adj.r2, b_mod2_adj.r2,
                              e_mod1_adj.r2, e_mod2_adj.r2)))

```

```

##
## =====
##                               Dependent variable:
##                               -----
##                               (1)      (2)      (3)      (4)
## -----
## treat                        0.016*** 0.022** 0.015*** 0.013**
##                               (0.005) (0.007) (0.004) (0.005)
##
## time                         -0.015** 0.002   -0.014** -0.001
##                               (0.005) (0.012) (0.005) (0.006)
##
## treat:time                   -0.007  -0.011  -0.004  -0.001
##                               (0.004) (0.007) (0.004) (0.005)
##
## Constant                     0.018*** 0.0003  0.019*** 0.007
##                               (0.005) (0.008) (0.004) (0.004)
##
## -----
## N                             2040     408     1275     255
## R squared                     0.229     0.534     0.283     0.358
## Adjusted R squared            0.194     0.457     0.238     0.18

```

```

## =====
## Note:                *p<0.05; **p<0.01; ***p<0.001
#####
### TABLE 11
#####

# To avoid confusion, remove all objects created for previous table
# Define a list of prefixes you want to remove
prefixes_to_remove <- c("p.btc","p.eth",
                        "b_","e_",
                        "btc_","eth_",
                        "lower_","upper_")

# Create a pattern that matches any of these prefixes at the beginning of object names
pattern <- paste0("^(", paste(prefixes_to_remove, collapse="|"), ")")

# Remove objects matching the pattern
rm(list=ls(pattern=pattern))

# Prep the data using the function
lower_bound = 1249
upper_bound = 1750
p.btc <- process_trading_data(df.btc, lower_bound = lower_bound, upper_bound = upper_bound)
p.eth <- process_trading_data(df.eth, lower_bound = lower_bound, upper_bound = upper_bound)

## Create two ranges of 50 and 10 dollars below the threshold for each
btc_range1 <- filter(p.btc, dollar_bins > 1449 & dollar_bins < 1500)
btc_range2 <- filter(p.btc, dollar_bins > 1489 & dollar_bins < 1500)

eth_range1 <- filter(p.eth, dollar_bins > 1449 & dollar_bins < 1500)
eth_range2 <- filter(p.eth, dollar_bins > 1489 & dollar_bins < 1500)

# Create difference-in-differences models for each range
btc_mod1 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),btc_range1)
btc_mod2 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),btc_range2)

eth_mod1 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),eth_range1)
eth_mod2 <- lm(prop_trades ~ treat*time + factor(id_2) + factor(m_d),eth_range2)

## Extract R^2, adjusted R^2, and N for each model
# mod1
b_mod1_r2 <- round(summary(btc_mod1)$r.squared,3)
b_mod1_adj.r2 <- round(summary(btc_mod1)$adj.r.squared,3)
b_N1 <- nrow(btc_range1)

# mod2
b_mod2_r2 <- round(summary(btc_mod2)$r.squared,3)
b_mod2_adj.r2 <- round(summary(btc_mod2)$adj.r.squared,3)
b_N2 <- nrow(btc_range2)

# mod1
e_mod1_r2 <- round(summary(eth_mod1)$r.squared,3)
e_mod1_adj.r2 <- round(summary(eth_mod1)$adj.r.squared,3)

```

```

e_N1 <- nrow(eth_range1)

# mod2
e_mod2_r2 <- round(summary(eth_mod2)$r.squared,3)
e_mod2_adj.r2 <- round(summary(eth_mod2)$adj.r.squared,3)
e_N2 <- nrow(eth_range2)

# Now calculate models for each range using robust standard errors
# clustered by exchange - trading pair
b_mod_robust <- coeftest(btc_mod1, vcov = vcovHC(btc_mod1, type="HC1"),
                        cluster = ~identitfier)
b_mod_robust2 <- coeftest(btc_mod2, vcov = vcovHC(btc_mod2, type="HC1"),
                          cluster = ~identitfier)

e_mod_robust <- coeftest(eth_mod1, vcov = vcovHC(eth_mod1, type="HC1"),
                        cluster = ~identitfier)
e_mod_robust2 <- coeftest(eth_mod2, vcov = vcovHC(eth_mod2, type="HC1"),
                          cluster = ~identitfier)

# Now use stargazer to create a Latex table using this information
stargazer(b_mod_robust,b_mod_robust2,
          e_mod_robust,e_mod_robust2,
          type = "text",
          omit=c("m_d","id_2"),
          star.cutoffs = c(0.05, 0.01, 0.001),
          add.lines = list(c("N",b_N1,b_N2,e_N1,e_N2),
                           c("R squared", b_mod1_r2, b_mod2_r2,
                               e_mod1_r2, e_mod2_r2),
                           c("Adjusted R squared", b_mod1_adj.r2, b_mod2_adj.r2,
                               e_mod1_adj.r2, e_mod2_adj.r2)))

```

```

##
## =====
##                               Dependent variable:
##                               -----
##                               (1)      (2)      (3)      (4)
## -----
## treat                        0.004    0.030*   0.003    0.015**
##                               (0.007)   (0.013) (0.010) (0.005)
##
## time                         -0.004   0.048*  -0.006   0.051
##                               (0.008)   (0.023) (0.013) (0.051)
##
## treat:time                   0.006   -0.004   0.010   -0.006
##                               (0.004)   (0.011) (0.011) (0.006)
##
## Constant                    0.013*  -0.008   0.015*  -0.0003
##                               (0.006)   (0.008) (0.007) (0.006)
##
## -----
## N                            2040     408     1275     255
## R squared                    0.122     0.31    0.092     0.247
## Adjusted R squared          0.081     0.195   0.035     0.039

```

```

## =====
## Note:                *p<0.05; **p<0.01; ***p<0.001
#####
### TABLE 12
#####

## Part 1: Data preparation

# To avoid confusion, remove all objects created for previous table
# Define a list of prefixes you want to remove
prefixes_to_remove <- c("p.btc","p.eth",
                        "b_", "e_",
                        "btc_", "eth_",
                        "lower_", "upper_")

# Create a pattern that matches any of these prefixes at the beginning of object names
pattern <- paste0("^(", paste(prefixes_to_remove, collapse="|"), ")")

# Remove objects matching the pattern
rm(list=ls(pattern=pattern))

## Separate by before and after regulatory change
df.btc_pre <- df.btc %>%
  filter(m_d < "07:10",
         type == "regulated")
df.btc_post <- df.btc %>%
  filter(m_d >= "07:10",
         type == "regulated")

df.eth_pre <- df.eth %>%
  filter(m_d < "07:10",
         type == "regulated")
df.eth_post <- df.eth %>%
  filter(m_d >= "07:10",
         type == "regulated")

## 2. Bitcoin analysis

## A. Pre

b_range1 = df.btc_pre[(df.btc_pre$base >= 250 & df.btc_pre$base < 750),]
b_range2 = df.btc_pre[(df.btc_pre$base >= 750 & df.btc_pre$base < 1250),]
b_range3 = df.btc_pre[(df.btc_pre$base >= 1250 & df.btc_pre$base < 1750),]

##Get estimates
b_r1 = estimate_beta(df.btc_pre, z_vector, binv, zstar=490, bins_excl_l=9, bins_excl_r=0)
b_r2 = estimate_beta(df.btc_pre, z_vector, binv, zstar=990, bins_excl_l=9, bins_excl_r=0)
b_r3 = estimate_beta(df.btc_pre, z_vector, binv, zstar=1490, bins_excl_l=9, bins_excl_r=0)

b_results = rbind.data.frame(b_r1,b_r2,b_r3)

b_results$t_statistic = abs(b_results$beta)/b_results$`standard error`
b_results[,c(2:4)] = sapply(b_results[,c(2:4)],rounding)

```

Table 1: Bitcoin Pre-Treatment Results

threshold	beta	standard error	t_statistic	count_transactions
490	5.051	2.326	2.172	15149
990	3.680	0.480	7.667	20903
1490	-4.661	0.571	8.162	5948

^a N exchanges = 2: N trading pairs = 4.

```

b_transactions = c(count(b_range1),count(b_range2),count(b_range3))
b_transactions = unlist(b_transactions)
b_results$count_transactions = b_transactions

# Total exchanges and trading pairs
b_N_exchanges <- sum(length(unique(df.btc_pre$exchange)))
b_N_trading_pairs <- sum(length(unique(paste0(df.btc_pre$exchange,df.btc_pre$s))))

# Create a footnote showing the number of exchanges and trading pairs
my_footnote1b <- paste0("N exchanges = ",b_N_exchanges,": N trading pairs = ",b_N_trading_pairs, ".")

# Display Table
kable(b_results, caption = "Bitcoin Pre-Treatment Results", format = "latex", booktabs = T) %>%
  kable_styling() %>%
  add_footnote(my_footnote1b)

## B. Post

b2_range1 = df.btc_post[(df.btc_post$base >= 250 & df.btc_post$base < 750),]
b2_rangb2 = df.btc_post[(df.btc_post$base >= 750 & df.btc_post$base < 1250),]
b2_range3 = df.btc_post[(df.btc_post$base >= 1250 & df.btc_post$base < 1750),]

##Get estimates
b2_r1 = estimate_beta(df.btc_post, z_vector, binv, zstar=490, bins_excl_l=9, bins_excl_r=0)
b2_r2 = estimate_beta(df.btc_post, z_vector, binv, zstar=990, bins_excl_l=9, bins_excl_r=0)
b2_r3 = estimate_beta(df.btc_post, z_vector, binv, zstar=1490, bins_excl_l=9, bins_excl_r=0)

b2_results = rbind.data.frame(b2_r1,b2_r2,b2_r3)

b2_results$t_statistic = abs(b2_results$beta)/b2_results$`standard error`
b2_results[,c(2:4)] = sapply(b2_results[,c(2:4)],rounding)
b2_transactions = c(count(b2_range1),count(b2_rangb2),count(b2_range3))
b2_transactions = unlist(b2_transactions)
b2_results$count_transactions = b2_transactions

# Total exchanges and trading pairs
b2_N_exchanges <- sum(length(unique(df.btc_post$exchange)))
b2_N_trading_pairs <- sum(length(unique(paste0(df.btc_post$exchange,df.btc_post$s))))

# Create a footnote showing the number of exchanges and trading pairs
my_footnote2 <- paste0("N exchanges = ",b2_N_exchanges,": N trading pairs = ",b2_N_trading_pairs, ".")

# Display Table
kable(b2_results, caption = "Bitcoin Post-Treatment Results", format = "latex", booktabs = T) %>%

```

Table 2: Bitcoin Post-Treatment Results

threshold	beta	standard error	t_statistic	count_transactions
490	-0.088	2.040	0.043	101523
990	3.146	0.945	3.328	116790
1490	-0.511	0.366	1.398	55521

^a N exchanges = 2: N trading pairs = 4.

```

kable_styling() %>%
add_footnote(my_footnote2)

## 3. Ethereum analysis

## A. Pre

e_range1 = df.eth_pre[(df.eth_pre$base >= 250 & df.eth_pre$base < 750),]
e_range2 = df.eth_pre[(df.eth_pre$base >= 750 & df.eth_pre$base < 1250),]
e_range3 = df.eth_pre[(df.eth_pre$base >= 1250 & df.eth_pre$base < 1750),]

##Get estimates
e_r1 = estimate_beta(df.eth_pre, z_vector, binv, zstar=490, bins_excl_l=9, bins_excl_r=0)
e_r2 = estimate_beta(df.eth_pre, z_vector, binv, zstar=990, bins_excl_l=9, bins_excl_r=0)
e_r3 = estimate_beta(df.eth_pre, z_vector, binv, zstar=1490, bins_excl_l=9, bins_excl_r=0)

e_results = rbind.data.frame(e_r1,e_r2,e_r3)

e_results$t_statistic = abs(e_results$beta)/e_results$`standard error`
e_results[,c(2:4)] = sapply(e_results[,c(2:4)],rounding)
e_transactions = c(count(e_range1),count(e_range2),count(e_range3))
e_transactions = unlist(e_transactions)
e_results$count_transactions = e_transactions

# Total exchanges and trading pairs
e_N_exchanges <- sum(length(unique(df.eth_pre$exchange)))
e_N_trading_pairs <- sum(length(unique(paste0(df.eth_pre$exchange,df.eth_pre$s))))

# Create a footnote showing the number of exchanges and trading pairs
my_footnote1 <- paste0("N exchanges = ",e_N_exchanges,": N trading pairs = ",e_N_trading_pairs, ".")

# Display Table
kable(e_results, caption = "Ethereum Pre-Treatment Results", format = "latex", booktabs = T) %>%
  kable_styling() %>%
  add_footnote(my_footnote1)

## B. Post

e2_range1 = df.eth_post[(df.eth_post$base >= 250 & df.eth_post$base < 750),]
e2_range2 = df.eth_post[(df.eth_post$base >= 750 & df.eth_post$base < 1250),]
e2_range3 = df.eth_post[(df.eth_post$base >= 1250 & df.eth_post$base < 1750),]

##Get estimates
e2_r1 = estimate_beta(df.eth_post, z_vector, binv, zstar=490, bins_excl_l=9, bins_excl_r=0)

```

Table 3: Ethereum Pre-Treatment Results

threshold	beta	standard error	t_statistic	count_transactions
490	5.684	1.751	3.247	16635
990	3.524	1.771	1.989	4189
1490	3.235	2.014	1.606	1609

^a N exchanges = 2: N trading pairs = 2.

Table 4: Ethereum EUR Results

threshold	beta	standard error	t_statistic	count_transactions
490	-0.383	0.782	0.490	107025
990	2.671	0.645	4.139	56844
1490	-0.454	1.282	0.354	20489

^a N exchanges = 2: N trading pairs = 2.

```
e2_r2 = estimate_beta(df.eth_post, z_vector, binv, zstar=990, bins_excl_l=9, bins_excl_r=0)
e2_r3 = estimate_beta(df.eth_post, z_vector, binv, zstar=1490, bins_excl_l=9, bins_excl_r=0)

e2_results = rbind.data.frame(e2_r1,e2_r2,e2_r3)

e2_results$t_statistic = abs(e2_results$beta)/e2_results$standard error
e2_results[,c(2:4)] = sapply(e2_results[,c(2:4)],rounding)
e2_transactions = c(count(e2_range1),count(e2_range2),count(e2_range3))
e2_transactions = unlist(e2_transactions)
e2_results$count_transactions = e2_transactions

# Total exchanges and trading pairs
e2_N_exchanges <- sum(length(unique(df.eth_post$exchange)))
e2_N_trading_pairs <- sum(length(unique(paste0(df.eth_post$exchange,df.eth_post$s))))

# Create a footnote showing the number of exchanges and trading pairs
my_footnote2 <- paste0("N exchanges = ",e2_N_exchanges,": N trading pairs = ",e2_N_trading_pairs, ".")

# Display Table
kable(e2_results, caption = "Ethereum EUR Results", format = "latex", booktabs = T) %>%
  kable_styling() %>%
  add_footnote(my_footnote2)

#####
### FIGURES 3 and 4
#####

## Part 1: Data preparation

# To avoid confusion, remove all objects created for previous table
# Define a list of prefixes you want to remove
prefixes_to_remove <- c("p.btc","p.eth",
                        "b_","e_",
                        "b2_","e2_")
```

```

    "btc_", "eth_",
    "my_",
    "lower_", "upper_")

# Create a pattern that matches any of these prefixes at the beginning of object names
pattern <- paste0("^(", paste(prefixes_to_remove, collapse="|"), ")")

# Remove objects matching the pattern
rm(list=ls(pattern=pattern))

# Prep the data using the function
lower_bound = 749
upper_bound = 1250
p.btc <- process_trading_data(df.btc, lower_bound = lower_bound, upper_bound = upper_bound)
p.eth <- process_trading_data(df.eth, lower_bound = lower_bound, upper_bound = upper_bound)

## Part 2: Bitcoin pre-trend plots

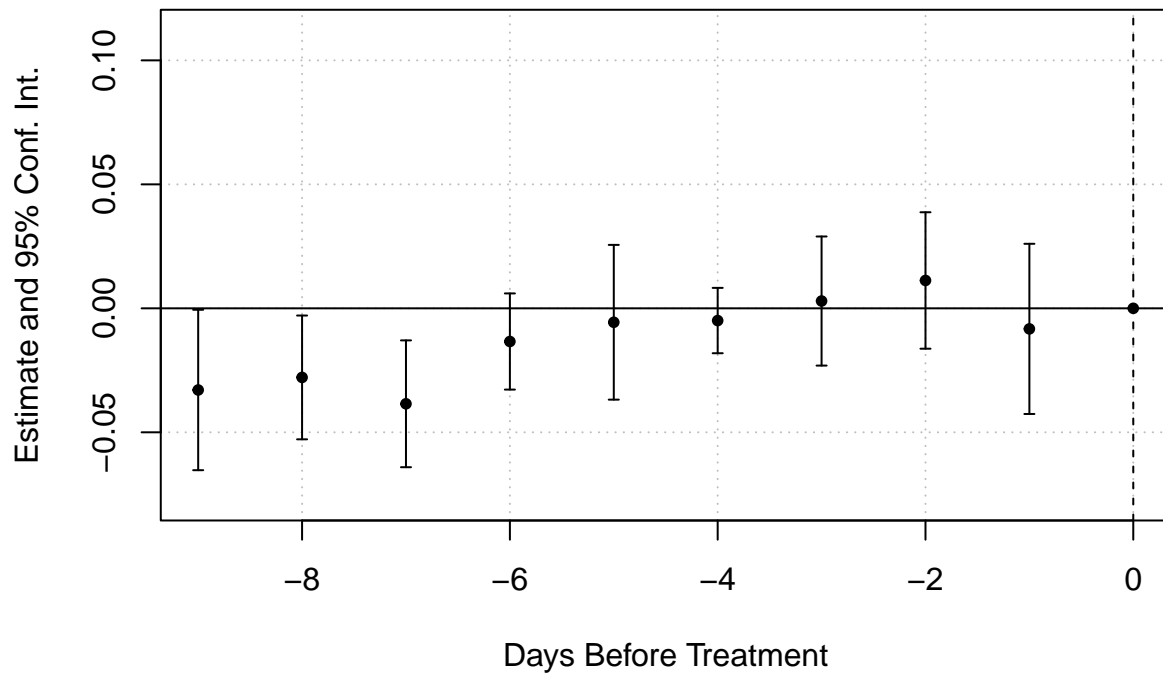
## A. 50 units below threshold
sub1 <- p.btc %>%
  filter(dollar_bins >= 950 & dollar_bins < 1000)

# Adjust time
sub1$time <- as.numeric(as.factor(sub1$m_d)) - 10
sub1$time_treat <- ifelse(sub1$time > -1, 1, 0)

# Create two-way fixed effects model
twfe_results <- fixest::feols(prop_trades ~ i(time, treat, ref = 0) | id_2 + time,
                             cluster = "id_2",
                             data = sub1)

# Generate plot
fixest::iplot(twfe_results,
              xlab="Days Before Treatment",
              main="",
              xlim=c(-9,0))

```



```

## B. 10 units below threshold

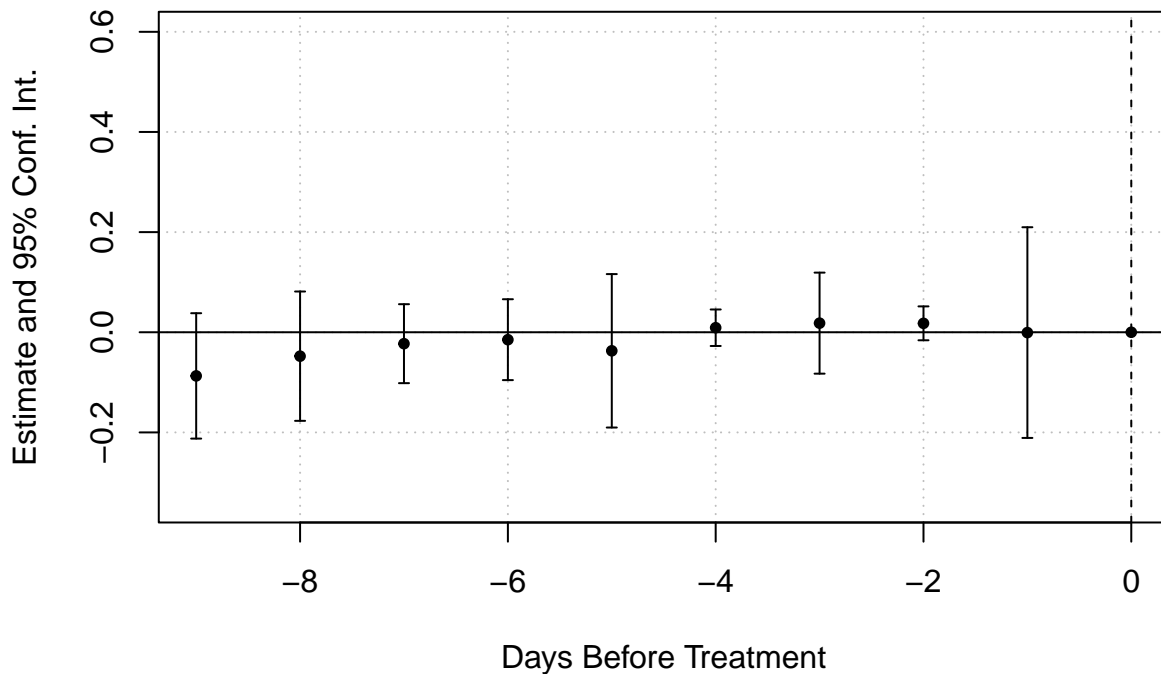
sub2 <- p.btc %>%
  filter(dollar_bins >= 990 & dollar_bins < 1000)

sub2$time <- as.numeric(as.factor(sub2$m_d)) - 10
sub2$time_treat <- ifelse(sub2$time > -1,1,0)

# Create two-way fixed effects model
twfe_results.2 <- fixest::feols(prop_trades ~ i(time, treat, ref = 0) | id_2 + time,
  cluster = "id_2",
  data = sub2)

# Generate plot
fixest::iplot(twfe_results.2,
  xlab="Days Before Treatment",
  main="",
  xlim=c(-9,0))

```



```
## Part 3: Ethereum pre-trend plots

# To avoid confusion, remove all objects created for previous plots
# Define a list of prefixes you want to remove
prefixes_to_remove <- c("sub", "twfe_")

# Create a pattern that matches any of these prefixes at the beginning of object names
pattern <- paste0("^(", paste(prefixes_to_remove, collapse="|"), ")")

# Remove objects matching the pattern
rm(list=ls(pattern=pattern))

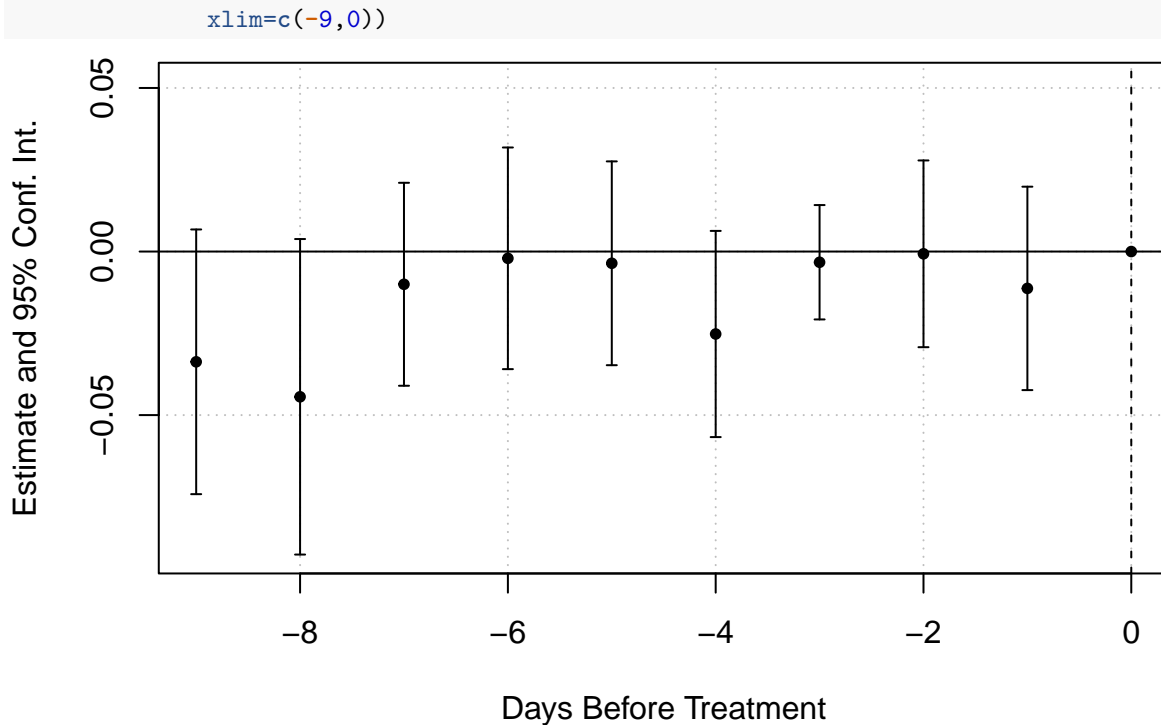
## A. 50 units below threshold

## First, do it for the 50 below the threshold
sub1 <- p.eth %>%
  filter(dollar_bins >= 950 & dollar_bins < 1000)

# Adjust time
sub1$time <- as.numeric(as.factor(sub1$m_d)) - 10
sub1$time_treat <- ifelse(sub1$time > -1, 1, 0)

# Create two-way fixed effects model
twfe_results <- fixest::feols(prop_trades ~ i(time, treat, ref = 0) | id_2 + time,
  cluster = "id_2",
  data = sub1)

fixest::iplot(twfe_results,
  xlab="Days Before Treatment",
  main="",
```



```
## B. 10 units below threshold

sub2 <- p.eth %>%
  filter(dollar_bins >= 990 & dollar_bins < 1000)

sub2$time <- as.numeric(as.factor(sub2$m_d)) - 10
sub2$time_treat <- ifelse(sub2$time > -1,1,0)

# Create two-way fixed effects model
twfe_results.2 <- fixest::feols(prop_trades ~ i(time, treat, ref = 0) | id_2 + time,
  cluster = "id_2",
  data = sub2)

fixest::iplot(twfe_results.2,
  xlab="Days Before Treatment",
  main="",
  xlim=c(-9,0))
```

